

Math 414-1 / 714-1
Homework 5: Supercoiling
The homework set is due on Thursday, April 3rd

I. Reading Assignment:

DNA topology by Bates and Maxwell, sections 2.1-2.5

II. Literature search:

- a. Klenin K. and Langowski J., Computation of writhe in modeling supercoiled DNA (2000); find the paper in PubMed, read it. Give a brief summary of the paper's contents. You will use this paper to complement your lecture notes (we will go into the details in class).
- b. Search review papers on DNA supercoiling; write a commentary of one of the papers

III. Using regular diagrams, illustrate the correspondence between overwinding of a short DNA molecule and changes in helical pitch and supercoiling. Repeat for unwinding.

IV. Consider a linear fragment of DNA. What atomic groups do you need to add to the end of the chain to form a closed DNA molecule?

V. Let A and B be two circular DNA molecules of different length, but with same linking number difference $\Delta Lk = +3$:

$$\text{Molecule A: } \Delta Lk = Lk_A - Lk_0^A = +3$$

$$N = 500\text{bp}$$

$$\text{Molecule B: } \Delta Lk = Lk_B - Lk_0^B = +3$$

$$N = 1,000,000\text{bp}$$

Compute the supercoiling densities σ_A and σ_B , and interpret your results.

VI. In *Escherichia coli* cells the DNA chromosome and all naturally occurring plasmids have supercoiling density $\sigma = -0.06$. Consider a bacterial plasmid of length 4361bp.

a) Calculate the linking number Lk of this plasmid, as well as the linking number difference $\Delta Lk = Lk - Lk_0$.

b) Is this plasmid relaxed, positively or negatively supercoiled? Argue using results from part a. Explain your answer. Do you know the name of this plasmid?